A MICROECONOMIC ANALYSIS OF PRODUCTIVITY IN THE MANUFACTURING INDUSTRY OF NORTH WEST

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ABSTRACT
This article studies the productivity in the manufacturing industry of the North West Province. Estimates of the Cobb-Douglas production function for the province's manufacturing industry are utilised and then applied to the industry's cost structure to determine whether the factors of production are optimally allocated.

It was found that the levels of labour productivity are continuously declining. Higher gains in output could have been achieved if expenditure on production factors were optimally allocated. What the optimal allocations should have been are then determined in monetary terms.

Finally, the paper accepts that the manufacturing industry is estimating market demand fairly accurately without stockpiling of supplies. The paper then determines what the level of optimisation of the capital and labour input base in the manufacturing industry should have been and what the extent of savings could be if production factors are optimally allocated in the North West Province's manufacturing industry.

OPSOMMING
Die produktiwiteit van die vervaardigingsnywerheid in die Noordwes Provinsie word in hierdie artikel bestudeer. 'n Cobb-Douglas produkisiefunksie word vir die vervaardigingsnywerheid van die provinsie geskat. Die resultate word dan op die nywerheid se kostestructuur toegepas om te bepaal of die produktiefaktore optimaal geallokeer is.

Daar is gevind dat die vervaardigingsnywerheid markvraag redelik akkuraat voorspel sonder ophoping van voorraade. Daar word dan bepaal wat die vlak van optimalisie van die kapitaal en arbeidsbasis in die vervaardigingsnywerheid behoort te wees. Hoeveel die besparings kan wees indien produktiefaktore optimaal geallokeer word in die vervaardigingsnywerheid van Noordwes Provinsie?

The optimal level of the labour and capital input base in the manufacturing industry of the North West Province is investigated in this study. It determines whether the industry was functioning at the optimal level, how much the deviation is costing the industry and how much could be gained when the input combination is rectified.

Van Zyl & Kleynhans suggested a unique way of determining productivity through the evaluation of the input combination of the factors of production in the issue of the Journal of Industrial Psychology of May 1995. This paper seeks to investigate that technique by applying it to the manufacturing industry of the North West Province. The excellence of this method lies in the fact that it expresses productivity or the loss thereof and the possible gains of higher productivity in monetary terms. As the findings are expressed in rand and cent planners can use them directly in their development strategies.

With the elimination of protective tariffs and the globalisation of the South African economy, optimal levels have to be striven for to survive increasing international competition. Future competitiveness is critically dependent on a higher level of cost efficiency and especially on a more productive labour and capital input.

Manufacturing in the province is important as a provider of employment and foreign revenue and it contributes towards the balance of payments and technological advancement. Manufacturing demands locally provided raw and intermediate materials and helps to alleviate of poverty in the region.

It is therefore important to be able to measure and quantify the extent of the perceived lack of productivity. The Cobb-Douglas efficiency criterion provides a straightforward instrument for this purpose. The findings should help industry, labour unions and other interest groups to comprehend the full implications of the low levels of productivity in the industry.

This article will commence with an overview of the economy of the North West Province and its manufacturing industry in particular. Then the theoretical concept of the efficiency criterion will be explained. Next a production function for manufacturing in the province will be estimated, which will provide the elasticities and other variables to estimate the optimal input ratios and efficiency criteria, based on historical achievements. Thereafter the optimal utilisation of the total cost outlay will be determined and lastly the optimal factor allocation warranted by the market demand will be determined. In each case the optimal input combination of the factors of production will be determined, the losses that occurred with the unproductive input combinations and possible gains in monetary terms. The paper concludes by evaluating the merits of the method applied, and suggestions will be formulated that could enhance manufacturing in the province.

THE ECONOMY OF THE NORTH WEST PROVINCE

The North West Province embraces 9.7 per cent of South Africa's soil and houses 8.6 per cent of the population. The population grows at a rate of 2.9 per cent and the region's GDP grows annually at only 1.2 per cent (1980–1991), which implies that the per capita income is declining (Erasmus, 1998:81-82)\(^1\).

The province provides 5.7 per cent of South Africa's GDP (1996). Manufacturing is contributing 10.35 per cent and it is growing at an annual rate of 4.01 per cent, which is the second best of all the provinces (Erasmus, 1998:81-82).

\(^1\) It is unfortunate that more recent statistics is not always available, but it serves to illustrate the general trends.

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The unemployment rate is 36.6 per cent (1994), which is four per cent above the national average (Schneider, 1998:85). In 1991 only 48.9 per cent of the extended labour force was formally employed. The low employment levels contribute to the high level of poverty in North West (DBSA, 1995:79).

The North West Province experienced employment growth of 0.55 per cent annually, between 1980 and 1991. The best employment growth rates were in finance, insurance & real estate, which grew by 4.42 per cent and manufacturing, where employment was growing at 2.66 per cent. These employment growth rates are still much less than their increase in production. This implies that jobless growth occurred in the North West. The only sectors in North West, which experienced negative employment growth were agriculture, mining & quarrying (DBSA, 1995:117).

The underdeveloped state of the North West’s manufacturing is not only evident in its relatively low contribution of twelve per cent to provincial GGP relative to 32 per cent in Gauteng (1998), but in the fact that the whole manufacturing sector is dominated by only three industrial sectors. Fabricated metals (51%), non-metallic minerals (21%) and food and beverage products (18%) are responsible for 90 per cent of the province’s manufacturing output.

Manufacturing is spatially concentrated with more than 80 per cent of the firms located in the Klerksdorp-Potchefstroom and Rustenburg-Brits districts, in close proximity to Gauteng and the Platinum SDI.

The three dominating industries in North West are all low technology medium-wage and resource-intensive products. The types of industry which would benefit from South Africa’s trade liberalisation and the GEAR strategy, like textiles and electronics, are absent from the province (Kleyhans, Naude & Suleman, 1998:46).

Similar trends emerge when looking at the value added and capital/labour ratios. In North West, only 60 per cent of manufacturing firms can be classified as high value added industries. In Gauteng it is 76 per cent. This suggests that technology is not as advanced in North West, and more importantly from an investment point of view, that profits are not as high as in Gauteng or other provinces (IDC, 1998a:75).

North West has a low degree of competitiveness. This does not bode well for attempts to encourage investment - especially FDI. Competitiveness is one of the fundamental determinants of investment and of decision by industrialists regarding location (Kleyhans et al. 1998:47).

North West has the lowest R & D expenditure per person annually (R 55 000 in real terms) compared to all other provinces (IDC, 1998a:75). In terms of R & D to GGP it ranks only ninth. However, the province boasts two universities (at Potchefstroom and Mafikeng) with significant R&D expertise and potential.

North West Province in particular has a low degree of internationalisation, and currently exports only 8.4 per cent of the manufacturing output. The province also does not have the same exposure to international tourism as most other provinces do. This province does, however, have much merit in its favour. The advantages to investors in the North West Province are the accessibility of water, electricity and labour. Water electricity, rent, labour, telephone, transport and airfreight is relatively less-expensive than is the case in the rest of the country. The province has a supply of supplier networks, support services, fresh produce, skilled and unskilled labour, infrastructure, internet & cell phones, roads and aviation.

The rail network comprises critical linkages in the national and regional networks. These are the North-South line (Harare-Johannesburg-Cape Town), the East-West line (Maputo-Rustenburg-Gaborone-Windhoek-Walvis Bay) and the Central corridor (Botswana-Zimbabwe-Zambia).

The airports at Pilansberg and Mafikeng are an important hub in the regional air network, especially as far as tourism is concerned. Mafikeng International Airport has amongst the highest ratings and designing standards in Southern Africa.

The meat processing industry has backward and forward linkage potential in such areas as feed production, animal science and breeding, feedlot development, and animal by-products for the fertiliser industry. The North West Province has a comparative advantage in this sector due to the extensive livestock production across the province, particularly in the Vryburg region, which has some of the most favourable conditions for cattle farming in the world, especially in terms of the absence of disease (Kleyhans et al. 1998:48).

Other significant industries are grain milling, edible oils and soaps (where the province can provide the potential investor ample access to raw materials), chemical products and the basic metal industry. An investigation by the Industrial Development Corporation in 1997 has found that North West has a comparative manufacturing advantage in the basic metal, food processing and chemicals industries; it was rated the top province in each of these industries (See Naudé, 1997:26 & Service group, 1997:25).

Given positive expected prospects for platinum, agro-industries and tourism in years to come, North West is set to experience a phase of growth and development. The province has already succeeded in turning the negative economic growth rates of the 1980s into high positive growth rates during the 1990s. Economic growth is expected to reach between five and six per cent per annum in future (IDC, 1998b:15).

Current real GGP per capita averages around R 4,385 per annum but is still characterised by high inequalities, especially between rural and urban areas (Erasmus, 1998:81-82). Human development in the North West Province shows severe spatial disparities. The infant mortality rate per 1 000 of the population is 43.3, which is nearly the same as the national average of 41.8 per cent (Schneider, 1998:85), but for some disadvantaged sections of the population, the infant mortality rates are up to seven times higher (DBSA, 1995:79). Life expectancy in North West is 64.1 years, which is about one year longer than the national average. The province has only 4.5 hospital beds per 1000 of the population, 0.7 less than the South African average; and the dependency rate in the province is about average at 1.6 (Naudé, 1998a:85).

The province has a Human Development Index (HDI) of only 0.543 (1993) compared to the national average of 0.64 (WEFA, 1996:41-45). This HDI is an improvement since 1980 when it was only 0.482 (Naudé, 1998b:66). The Gini coefficient is about average at 0.6 in the North West Province (Whiteford, 1995:21), but it still indicates inequality in the distribution of income and a huge challenge to economists and the authorities in the province. Among the population in the province 41.3 per cent live below the absolute poverty line and the poverty situation is even more acute in the rural areas (Naudé, 1998b:66 & DBSA, 1995:a:79).

The structure and context in which manufacturing operates in the North West Province’s economy was sketched above. In the following section the theoretical concept of the efficiency criterion will be explained to demonstrate how this study was done.

THE EFFICIENCY CRITERION

The theoretically purist and most widely used production function is the Cobb-Douglas function (Van Zyl 1995:6) which

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7 Being competitive indicates an ability to design, produce and market goods and services that are more appealing, of better quality and/or less expensive than those of competing suppliers (ITRISA, 2001:9)
states the relationship of labour (L) and capital (K) to output (Q) as: \( Q = a K^{\alpha} L^{\beta} \). The level of technology is indicated by \( \alpha \). Parameter \( \alpha \) is the output elasticity of capital and \( \beta \) the output elasticity of labour. Parameter \( \beta \) denotes the percentage change in output as a result of a percentage change in labour input, keeping capital constant (Cobb & Douglas, 1928:139-140).

The Cobb-Douglas production function is estimated by converting the function \( Q = a K^{\alpha} L^{\beta} \) to \( Q = \log a + \alpha \log K + \beta \log L \). By means of linear regression analysis parameters \( \alpha \) and \( \beta \) are determined. The marginal products of labour and capital are respectively \( MP_L = \beta (Q/K) \) and \( MP_K = \alpha (Q/K) \). The optimal cost efficient utilisation of production factors is obtained at the point where the last Rand is spent all factors yields equal marginal products:

\[ (MP_L/w) = (MP_K/r) \]

where \( w \) is the unit wage cost and \( r \) the unit cost of capital. The estimated production function can now be used to determine whether the input combination of an industry is optimal or sub-optimal (Van Zyl & Kleynhans, 1995:6).

When \( MP_L/MP_K < w/r \) it is an indication of over-utilisation of labour, indicating a decline in labour productivity. On the other hand, if \( MP_L/MP_K > w/r \), capital is over-utilised, indicating a decline in the productivity of the capital goods used and an over-utilisation of labour, ceteris paribus. The marginal rate of technical substitution of labour for capital is:

\[ \text{MRTS} = \frac{MP_K}{MP_L} = \frac{\beta (Q/K)}{\alpha (Q/K)} = \frac{\beta}{\alpha} \]

This is an indication of over-utilisation when more is spent on labour than on capital goods in the production process, and ceteris paribus a decline in labour productivity. The next step is to quantify the decline in labour productivity in terms of cost wastage (in Rand).

The optimal input ratio of labour and capital (\( z \)) must be such that \( K/L = (\omega/\alpha)/(\beta r) \). The optimal allocation of the labour input can be calculated from the optimal input ratio. Thus \( L_z = (\beta r K)/(\alpha \omega) \). The optimum allocation of the labour input can also be derived from the isocost line for a specific cost outlay \( C = rK + wL \) and \( L = (C-rK)/w \).

Levels of production where \( \Psi = 0 \) are rarely found in practice. Should the calculations show no optimum input allocation, it must be determined whether the calculated \( \Psi \) is significantly different from 0. This is done by means of a t-test. The calculated t-statistic is \( t = \Psi/S\Psi \). \( S\Psi \) is the estimated \( \Psi \)'s own standard error and the estimated variance of \( \Psi \) can be calculated as:

\[ \text{Var}(\Psi) = \left( \frac{K}{L} \right)^2 \text{Var}(\beta) + (w/r)^2 \text{Var}(\omega) - 2 \left( \frac{K}{L} \right) (w/r) \text{ Cov}(\omega, \beta) \]

The estimated standard error of \( \Psi \) is:

\[ S\Psi = \sqrt{\text{Var}(\Psi)} \]

The absolute t-value of \( \Psi \) is then calculated. Should it exceed the critical t-value, it can be said that \( \Psi \) is significantly different from zero (Maurice & Smithson, 1985:128-130).

When evaluating the optimum total cost outlay, it is important to take note of the intensity factor and the factor demand equations, derived from the Cobb-Douglas function. The intensity factor is \( \beta/\alpha \); the higher this ratio the more labour intensive the production technique (Koutsoyiannis, 1979:65). When \( \Psi = 0 \), \( \beta K/L = \alpha (w/r) \) or

\[ L = (K/\alpha)/r \]

Substituting \( K \) and \( L \) in the production function the factor demand equations are derived in terms of output and relative factor prices \( L_d = \left[ Q/L (r/w) \beta/\alpha \right]^{1/(\beta-\alpha)} \) (Heathfield, 1987:82).

The low levels of labour productivity in the industry over the period 1970-1995 had an adverse effect on the output level. From the results (see table 2) it is evident that a better utilisation (input mix) of the cost outlay would have resulted in a higher output level.

<table>
<thead>
<tr>
<th>Year</th>
<th>Output over-utilisation</th>
</tr>
</thead>
<tbody>
<tr>
<td>1970</td>
<td>-1.385.243</td>
</tr>
<tr>
<td>1971</td>
<td>-45.154</td>
</tr>
<tr>
<td>1972</td>
<td>-57.199</td>
</tr>
<tr>
<td>1973</td>
<td>12.747.374</td>
</tr>
<tr>
<td>1974</td>
<td>13.1072</td>
</tr>
<tr>
<td>1975</td>
<td>20.52269</td>
</tr>
<tr>
<td>1976</td>
<td>30.88467</td>
</tr>
<tr>
<td>1977</td>
<td>90.51764</td>
</tr>
<tr>
<td>1978</td>
<td>-574.411</td>
</tr>
<tr>
<td>1979</td>
<td>18.11745</td>
</tr>
<tr>
<td>1980</td>
<td>29.26706</td>
</tr>
<tr>
<td>1981</td>
<td>322.1764</td>
</tr>
<tr>
<td>1982</td>
<td>64.9608</td>
</tr>
<tr>
<td>1983</td>
<td>-52.27722</td>
</tr>
<tr>
<td>1984</td>
<td>-24.70522</td>
</tr>
<tr>
<td>1985</td>
<td>-151.745</td>
</tr>
<tr>
<td>1986</td>
<td>68.55199</td>
</tr>
<tr>
<td>1987</td>
<td>-197.723</td>
</tr>
<tr>
<td>1988</td>
<td>-94.1441</td>
</tr>
<tr>
<td>1989</td>
<td>-720.424</td>
</tr>
<tr>
<td>1990</td>
<td>-117.088</td>
</tr>
<tr>
<td>1991</td>
<td>-102.598</td>
</tr>
<tr>
<td>1992</td>
<td>-54.3686</td>
</tr>
<tr>
<td>1993</td>
<td>-1300.21</td>
</tr>
<tr>
<td>1994</td>
<td>-94.753</td>
</tr>
<tr>
<td>1995</td>
<td>-185.328</td>
</tr>
</tbody>
</table>

* Appreciation is expressed to Prof. Dr. JHP van Heerden for his assistance in estimating the production function; and assistant PJ Fourie for his preliminary investigation of the theme.
The possible optimal output gain was calculated for every year since 1970. For example, 1995: \( K = \text{R}1.484\text{m}; L = 57.345; w = 15.608; r = 0.0461; \Psi = -185.578 \) indicating an over-utilised labour situation with declining productivity. The true K/L ratio employed was \( K/L = 12.98433 \), while the optimal ratio should have been: \( (K/L)_o = \psi/aL \approx \) 37,825 indicating that the output of productive labour input base was sub-optimal.

The money spent on the factors of production was: \( C = rK + wL; C = \text{R}895.13\text{m} \)

The optimal input levels of capital and labour should have been:

\[ K_o = (\alpha C)/(\epsilon e) = \text{R}101.82\text{m} \text{ where } \epsilon = (\alpha + \beta) \text{ and } L_o = (\beta K)/(\omega w) = 27385 \text{ workers}. \]

Test: \( K_o/L_o = 37.825 \)

The level of production was calculated as: \( Q = aK^\epsilon L^\beta \)

The amount produced in that year was: \( Q_{true} = \text{R}3100.272\text{m} \), but at the point of optimisation \( Q_o = \text{R}271.33\text{m} \) could have been produced utilising the same cost outlay. The inefficiency output loss was: \( Q_o - Q_{true} = \text{R}68.23\text{m} \) where "O" indicates optimal and "true" the amount that was really occurred in that year.

The inefficient labour component is calculated as: \( L_{true} - L_o = 29.959 \text{ excess workers} \)

Table 2 shows the possible output wasted in each year (1987-1995) and the unproductive labour that was employed at the non-optimal factor allocation and total cost outlay levels.

<table>
<thead>
<tr>
<th>Year</th>
<th>Output loss (R mil.)</th>
<th>Unproductive labour (excess workers)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1987</td>
<td>300.3</td>
<td>32223</td>
</tr>
<tr>
<td>1988</td>
<td>210.7</td>
<td>34020</td>
</tr>
<tr>
<td>1989</td>
<td>658.8</td>
<td>34526</td>
</tr>
<tr>
<td>1990</td>
<td>244.9</td>
<td>34997</td>
</tr>
<tr>
<td>1991</td>
<td>222.8</td>
<td>34309</td>
</tr>
<tr>
<td>1992</td>
<td>146.3</td>
<td>32219</td>
</tr>
<tr>
<td>1993</td>
<td>811.9</td>
<td>30919</td>
</tr>
<tr>
<td>1994</td>
<td>187.9</td>
<td>30144</td>
</tr>
<tr>
<td>1995</td>
<td>268.2</td>
<td>29960</td>
</tr>
</tbody>
</table>

From the table, it is obvious that the calculated output loss as a result of the employment of unproductive labour remained relatively high over the entire period.

**OPTIMAL FACTOR ALLOCATION ACCORDING TO MARKET DEMAND**

Producing a higher output when an alternative optimal input combination is applied at the same cost-outlay would be unwise. Motor vehicles manufactured in South Africa are, for instance, sold within six weeks (Van Zyl & Kleynhans, 1995:8) to produce more would be a waste. The assumption in this paper is that manufacturers are already supplying what the market currently demands. It is therefore better to continue manufacturing the same amount of output, but at an optimal input combination of production factors.

When an optimal factor allocation at a given labour and capital cost has been determined for a particular cost outlay, it can be used to determine the optimal factor allocation warranted by the market demand.

The optimal amount of labour in the industry required to meet market demand can be calculated by the use of the formula \( L_{Df} = \sqrt{Q_{Df}/Z} - L \) where \( Z = \text{optimal K/L = (aw)/(3r)} \). The optimal capital input can be determined by \( K_{Df} = \sqrt{Q_{Df}/(aL^3)} \) (Van Zyl & Kleynhans, 1995:8-10).

Table 3 lists the non-productive labour component per level of market demand and the possible cost gain as a result of better factor utilisation, for each year during 1978-1995. It can be seen from Table 3 that the manufacturing industry is burdened by a significant number of non-productive labourers. These figures are disturbing when compared with the relevant facts. Real wages increased relatively, while the number of non-productive labourers had increased. This is an indication of a continuous decline in labour productivity.

<table>
<thead>
<tr>
<th>Year</th>
<th>Unproductive labour (R mil. = real prices)</th>
<th>Possible cost gain with less labour employed (R mil. = real prices)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1987</td>
<td>61609</td>
<td>146.8146</td>
</tr>
<tr>
<td>1988</td>
<td>6093</td>
<td>62.93753</td>
</tr>
<tr>
<td>1989</td>
<td>60720</td>
<td>321.6911</td>
</tr>
<tr>
<td>1990</td>
<td>60968</td>
<td>199.2662</td>
</tr>
<tr>
<td>1991</td>
<td>65651</td>
<td>221.7978</td>
</tr>
<tr>
<td>1992</td>
<td>61654</td>
<td>44.95409</td>
</tr>
<tr>
<td>1993</td>
<td>59172</td>
<td>6417.455</td>
</tr>
<tr>
<td>1994</td>
<td>58254</td>
<td>204.0643</td>
</tr>
<tr>
<td>1995</td>
<td>57330</td>
<td>376.2697</td>
</tr>
</tbody>
</table>

**SUMMARY AND CONCLUSIONS**

A) Evaluation of the Method Used

The Cobb-Douglas efficiency criteria and in particular its extensions, serve as effective and useful instruments to measure and quantify the extent of a decline in labour productivity in a particular industry.

The method is easy and economical to apply. More elaborate methods to obtain more accurate findings, better production functions and adjusting the figures to include changes in technology do not yield better results (see e.g. Kleyhnans, 1996:15). The fact that it measures productivity in Rand and Cent makes this method unique.

The method gives development managers a useful instrument when planning, as it gives the exact number of unproductive labour units and indicates the value of capital that should optimally be applied and the loss due to unproductivity in specific monetary terms. It also indicates what returns can be gained in Rand and Cent terms. In this regard it is not only an indication of the problem of unproductivity but also suggests part of the solution.

The method utilises real values and when real interest rates are negative it is impossible to draw roots when applying it and thus makes this method useless for those years. Alternative interest and inflation rate series might then be employed like the BA rate or CPI, but this will be less accurate. As companies gain tax gains on their levels of depreciation, it is very difficult to determine the true value of depreciation. Companies are also reluctant to release their production figures to others for research purposes. Indexes are, however, more readily available and the same technique could be employed to determine the percentages of unproductive labour and the percentages with which inputs should change and how that will alter production figures and costs. Within firms this method can, however, be used with ease as well as by investment institutions where firms have to declare their figures to obtain funds.

B) Productivity in the North West Province

The results of the efficiency criteria measurements do indeed substantiate the view that the continuous decline in labour productivity in the manufacturing industry of North West is one of the more important causes of rising market prices. The key challenge facing all those associated with the industry is the improvement of labour productivity at a time when the overall productivity trend remains under pressure and wages and other costs have been rising at a faster rate than those of the overseas competitors have. The alternative is to employ more capital goods, mechanise, implement robotics and re-trench those unproductive labourers.
The demands of the labour unions have probably compelled the industry to employ more labour at higher wage levels than would have been the case had management been at liberty to act more rationally. The low level of productivity per worker can probably also be attributed to the low worker ethics generally prevalent in the South African work force. The findings of this paper agree with those of Van Zyl & Kleynhans (1995:8) and studies like the Riley Report (IDC, 1993:99–102) of the Motor Industry Task Group that South African industries are too labour intensive. Since 1995 major changes and restructuring have also occurred resulting in job losses, which has worsened the situation. It did however raise competitiveness, which might create more employment in the longer term. Should the decline in labour productivity remain unchallenged, thousands of workers will have to be retrenched in order to bring unit cost down and make the industry more competitive.

REFERENCES

IDC see Industrial Development Corporation.